## Part II

## Total 40 points

(10)

1. Using the method discussed in class, convert the following CFG to one in Chomsky Normal Form. Show every step.

$$
\mathrm{G}=(\{\mathrm{S}, \mathrm{X}\},[\mathrm{a}, \mathrm{~b}\},\{\mathrm{S} \rightarrow \mathrm{bX}, \mathrm{X} \rightarrow \mathrm{XaX} \mid \varepsilon\}, \mathrm{S})
$$

(10)
2. Using the method discussed in class, for the following CFG G, write an equivalent CFG G' such that $\mathrm{G}^{\prime}$ does not contain unit productions. Show every step, including how to get UNIT sets.

$$
\begin{aligned}
& \mathrm{G}=(\{S, A, B, W, X, Y, Z\},\{a, b\}, P, S), \text { where } \\
& P=\{S \rightarrow X Y, A \rightarrow \mathrm{aA}|\mathrm{bA}| \mathrm{A}|\mathrm{~B}, \mathrm{~B} \rightarrow \mathrm{Ba}| \mathrm{Bb}|\mathrm{a}| \mathrm{b}, \mathrm{~W} \rightarrow \mathrm{Z}, \\
& \mathrm{X} \rightarrow \mathrm{Zb}|\mathrm{~b}, \mathrm{Y} \rightarrow \mathrm{bW}| \mathrm{b}, \mathrm{Z} \rightarrow \mathrm{AB}|\mathrm{~A}| \mathrm{B}\}
\end{aligned}
$$

(10)
3. Using the method discussed in class, construct a CFG G"which is equivalent to the following CFG G'and does not have useless symbols.
Show every step, including how to get REACH set and so on.
$G=(V, \Sigma, P, S)$, where $V=\{S, A, B, C, D, U, V, W, X, Y\}$,
$\Sigma=\{\mathrm{a}, \mathrm{b}, \mathrm{c}, \mathrm{d}, \mathrm{e}, \mathrm{f}, \mathrm{g}, \mathrm{h}, \mathrm{i}, \mathrm{j}, \mathrm{k}, \mathrm{m}, \mathrm{n}, \mathrm{o}\}$,
$\mathrm{P}=\{\mathrm{S} \rightarrow$ gAe laYB $|\mathrm{CY}, \mathrm{A} \rightarrow \mathrm{bBY}|$ ooC, $\mathrm{B} \rightarrow \mathrm{dd}|\mathrm{D}, \mathrm{C} \rightarrow \mathrm{jVB}| \mathrm{gi}$, $\mathrm{D} \rightarrow \mathrm{n}, \mathrm{U} \rightarrow \mathrm{kW}, \mathrm{V} \rightarrow \mathrm{baXXX} \mid \mathrm{oV}, \mathrm{W} \rightarrow \mathrm{c}, \mathrm{X} \rightarrow \mathrm{fV}, \mathrm{Y} \rightarrow \mathrm{Yhm}\}$.

